

“QCD AND STANDARD MODEL”
Problem Set 8

1. W boson decay

In this exercise you will compute the decay rate for the process $W \rightarrow e\bar{\nu}$. The relevant interaction term is

$$\frac{g}{\sqrt{2}} W_\mu^- \bar{e}_L \gamma^\mu \nu_L = \frac{g}{\sqrt{2}} W_\mu^- \bar{e} \gamma^\mu \frac{1}{2} (1 + \gamma_5) \nu .$$

In what follows, the electron and neutrino should be taken as unpolarized, i.e. you should sum over all polarizations. For simplicity, take the W at rest. You can assume that the electron and neutrino are massless (their masses are negligible compared to their energies since $M_W \simeq 80$ GeV).

W boson polarization vectors :

- *positive z direction* $e_T^\mu(+)$ = $\frac{1}{\sqrt{2}}(0, 1, i, 0)$
- *negative z direction* : $e_T^\mu(-)$ = $\frac{1}{\sqrt{2}}(0, 1, -i, 0)$
- *Longitudinally polarized* : $e_L^\mu(0)$ = $(0, 0, 0, 1)$

- a) Compute the partial differential decay rate and the total decay rate for the $W \rightarrow e\bar{\nu}$ process, with W polarized in the positive z direction.
- b) Repeat the same for the W boson polarized in the negative z direction.
Is the total decay rate the same as before? Why?
- c) Now, compute the same for the longitudinally polarized W boson (zero spin component in the z direction). Is the total rate the same as before? Why?
- d) Compute the total decay rate for an unpolarized W. Is it the same as before? Why?
- e) Compute the total decay rate of W into all SM quarks and leptons (assume that all are massless for simplicity). Take three generations of fermions and recall that the top quark is very heavy - heavier than the W boson. Take $g^2/4\pi = 1/30$ and $M_W = 80$ GeV.

Take into account the difference between quarks and leptons (quarks carry three colors). Compare with the PDG experimental result :

<http://pdg.lbl.gov/2017/tables/rpp2017-sum-gauge-higgs-bosons.pdf>.

We expect a small error since the τ lepton and b quark masses are not completely negligible.

2. Higgs boson decay to fermions

The Higgs Yukawa coupling to fermions is given by

$$\mathcal{L}_Y = \frac{g}{2} \frac{m_f}{M_W} h \bar{f} f .$$

Find the decay rate for the Higgs into a fermion-antifermion pair. Account for the situation $f =$ quark.