

# Neutrino Physics Course

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## Lecture I


LMU

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Spring 2022

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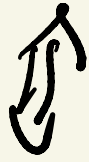
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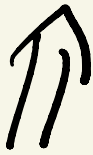
# Why neutrino?

- Essence of neutrino (mass) physics  
 $SM \Rightarrow m_\nu = 0$  SM = Standard Model
- $\nu$  mass  $\rightarrow$  due to new physics  
(Beyond the SM = BSM)
- P violation = max of it all  
fell and rise of parity
- Left-Right (LR) Symmetric Model = LR SM

LRSM: a (the?) theory of  $\nu$  mass



SM: theory of charged fermions  
(+ W, Z) masses



Higgs mechanism

Holy Grail: quest to grasp  
origin and nature of  
 $\nu$  mass



violation of lepton number  
(LNV)

$$\left| \begin{array}{l} e = \text{lepton} \\ \nu = \text{---} \end{array} \right.$$



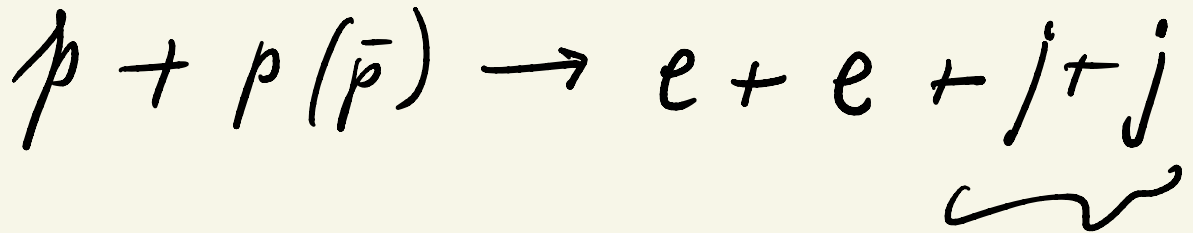
$$\Delta L = 2$$

- neutrino-less double beta decay

( $0\nu 2\beta$ )



- NS process = eucloy at LHC

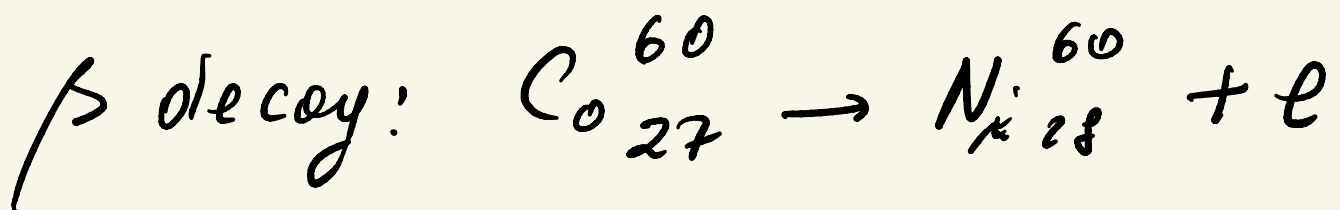


CMS + ATLAS

jets

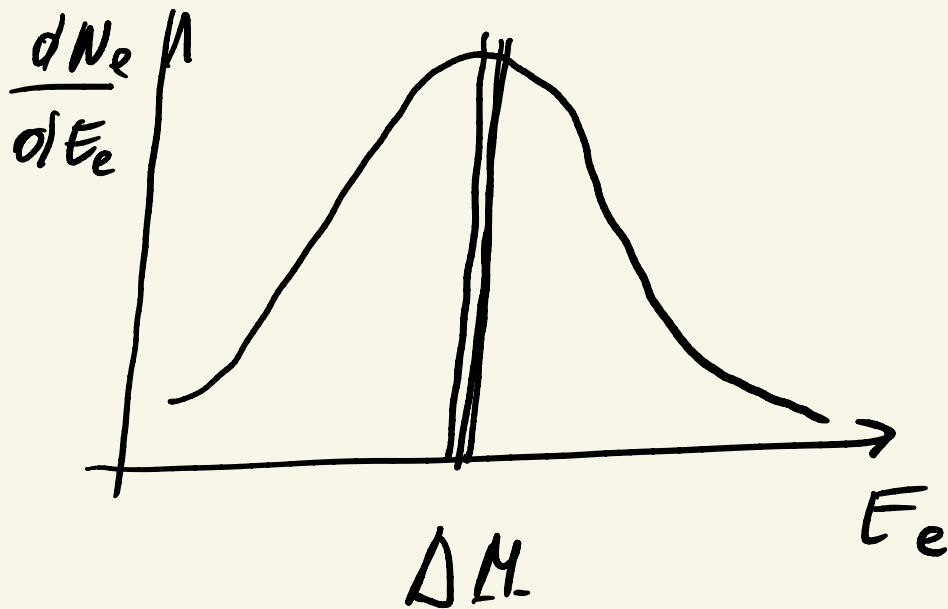
## History of $\nu$ birth

Chadwick 1914 - 20's



$$\Delta M = E_e = \text{fixed}$$

$\Downarrow$



Bohr:  $\Delta E \neq 0$

Pauli 1930 4/12

Postcard  $\rightarrow$  Tübingen conf.

$\exists$  neutron ( $Q=0$ )

1932 Chadwick  $\Rightarrow$  neutron

$\rightarrow$  neutrino (= little)

neutrino)

$$m_\nu \leq \text{MeV} \quad \text{early days}$$

today:  $m_\nu \leq \text{eV}$

KATRIN

$$m_\nu = 0 \quad ??$$

EM:

$$e A_\mu j_{em}^\mu = \mathcal{L}_{int}$$

$$e = \frac{1}{3}$$

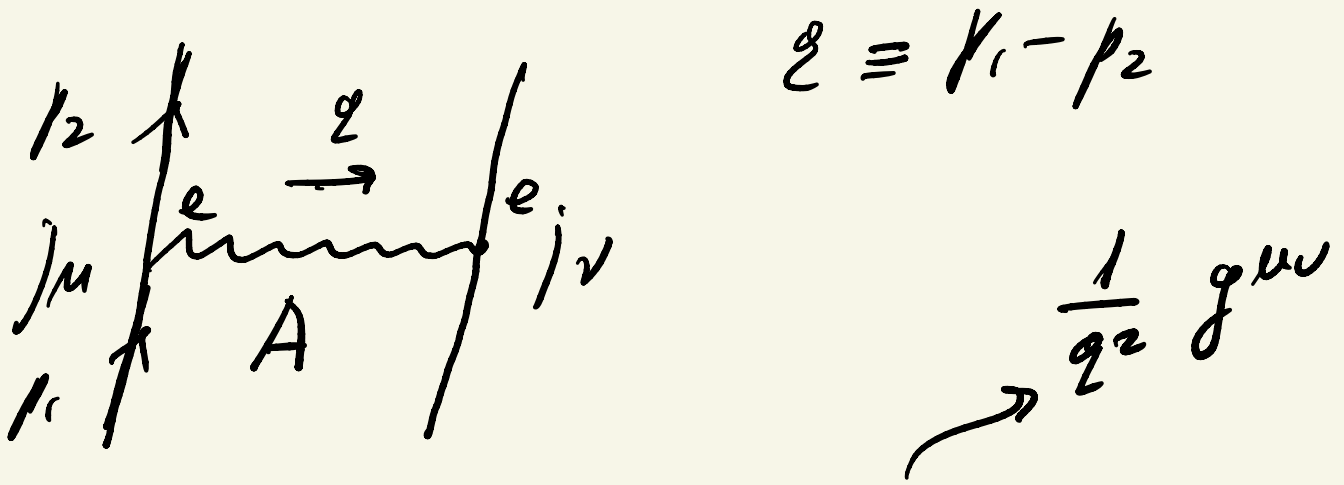
$$j_{em}^\mu = \bar{\psi} \gamma^\mu Q_{em} \psi$$

$$Q_{em} \psi = Q_\psi \psi$$

$$e: Q_e = -1$$

$$p: Q_p = +1$$

$$u: Q_u = 0$$



$$\Rightarrow \mathcal{H}_{\text{eff}}^{e\mu} = j_{\mu}^{e\mu} \Delta^{\mu\nu} j_{\nu}^{e\mu}$$

$$\frac{1}{g^2} j_{\mu}^{e\mu} j_{\mu}^{e\mu}$$

Could I guess it?

Lorentz symmetry:  $\mathcal{F}(g^2)$



$$\text{Exp. } m_A \leq 10^{-14} \text{ eV}$$

$$A = \gamma \\ = \text{photon}$$

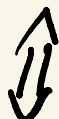
$$\Leftrightarrow \nu_{ew} \simeq \frac{1}{v} e^{-m_A r}$$

$$\simeq 1/v$$

$$\text{SM: } m_A = 0$$

1934 Fermi

$$j_w^\mu = \bar{p} \gamma^\mu n + \bar{\nu} \gamma^\mu e$$



$$n \rightarrow p + \underbrace{e + \bar{\nu}_e}_{\Delta L = 0}$$

$$\mathcal{H}_{\text{eff}}^F \approx \frac{1}{\Lambda_F^2} j^\mu \bar{j}_\mu \equiv \frac{G_F}{\sqrt{2}} j \bar{j}$$

$$\Leftrightarrow \mathcal{L}_{\text{int}} = g/\sqrt{2} j^\mu W_\mu^+ + \text{h.c.}$$

$$\frac{G_F}{\sqrt{2}} = \frac{1}{\Lambda_F^2} \approx 10^{-5} \text{ GeV}^{-2}$$

$$\Lambda_F \approx 300 \text{ GeV}$$

$$\boxed{g \approx \text{MeV}}$$

$$g(\text{LHC}) \approx 10^4 \text{ GeV} \leftarrow$$

units       $c = \frac{h}{h} = 1$

$$d(t) = d(L) \quad [t] = [L]$$

$$\frac{h}{h} = 1 \Leftrightarrow d(mvL) = 0$$

$$\Rightarrow \boxed{[m] = [L]^{-1}}$$

$$S = \int \mathcal{L} d^4x \quad d(S) = [S] = 0$$

$$\Rightarrow d(\mathcal{L}) = d(L)^{-4} \\ = d(m)^4$$

$$d(\mathcal{L}) = 4$$

units of mass

$$\mathcal{L}_D = i \bar{\psi} \gamma^\mu \partial_\mu \psi - m \bar{\psi} \psi$$

$$\bar{\psi} = \psi^\dagger \gamma^0$$

$$\Rightarrow d(\psi) = 3/2 \Rightarrow d(j) = 3$$

$$\left( \begin{array}{c} \Downarrow \\ d(A) = 1 \end{array} \right)$$

$$\mathcal{H}_{\text{eff}}^{\text{ew}} = f(e^2) \underbrace{j j}_{d=6}$$

$$d(f(e^2)) = -2$$

$$\Rightarrow f(e^2) = \frac{1}{e^2}$$

em:  $1/q^2$   $q = \text{MeV}^-$

weak:  $1/\Lambda_F^2$   $\Lambda_F \approx 300 \text{ GeV}$

$$\frac{\sigma_w}{\sigma_{em}} \approx ?$$

em:  $\sigma_{em} \approx \frac{e^2}{q^2} \rightarrow$

weak:  $\sigma_w \approx G_F^2 q^2 \quad (q > \text{MeV})$

$\text{left} \approx (G_F) j_w j_w$   $G_F \approx \frac{1}{\Lambda_F^2}$

$$\frac{\sigma_w}{\sigma_{eu}} \approx G_F^2 q^4$$

$$\approx 10^{-10} \cdot 10^{-12} \approx 10^{-22} \quad \text{! !}$$

Melfo, G.C.

Neutrino: . . . .

of about protagonist

• mean free path

$$\lambda_e \approx \frac{1}{\sigma \cdot v \cdot n} \approx 10^{-2} \text{ au}$$

$\nearrow$  cross section     $\uparrow$  velocity     $\rho$  density

$$n \approx 10^{24} / \text{cm}^3$$

$$\lambda_\nu \approx 10^{20} \text{ au}$$

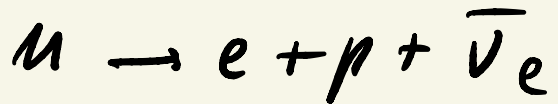
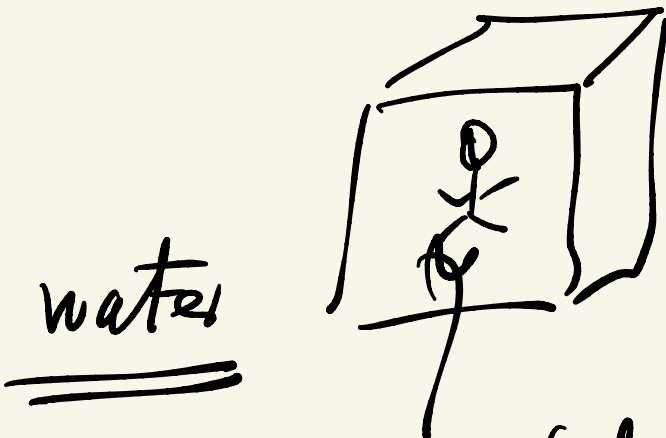
$$\rightarrow 10^7 d_{SE}$$

Sun-earth

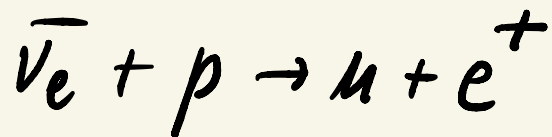
PonteCorvo: reactors '40

Cowen, Reines  
→ '56

$$\Phi = 10^{13} / \text{cm}^2 \text{ sec}$$



detect



$$V \approx 10^5 \text{ m}^3$$

"good old days"

$$\#_{\text{events}} = \Phi \sigma_w \cdot n \cdot V$$

$$\sigma_w \approx G_F^2 q^2 \approx 10^{-10} \cdot 10^{-6} \text{ GeV}^{-2}$$

$$\left( v_c (\text{proton}) \approx 10^{-14} \text{ cm} \quad (\pi) \right)$$

$$\approx \frac{1}{m_p} \approx \text{GeV}^{-1}$$

$$\boxed{m_p \approx m_n \approx \text{GeV}} \quad (m_n > m_p)$$

$$\text{GeV}^{-2} \approx 10^{-28} \text{ cm}^2$$

$$\Rightarrow \boxed{\sigma_w \approx 10^{-44} \text{ cm}^2}$$



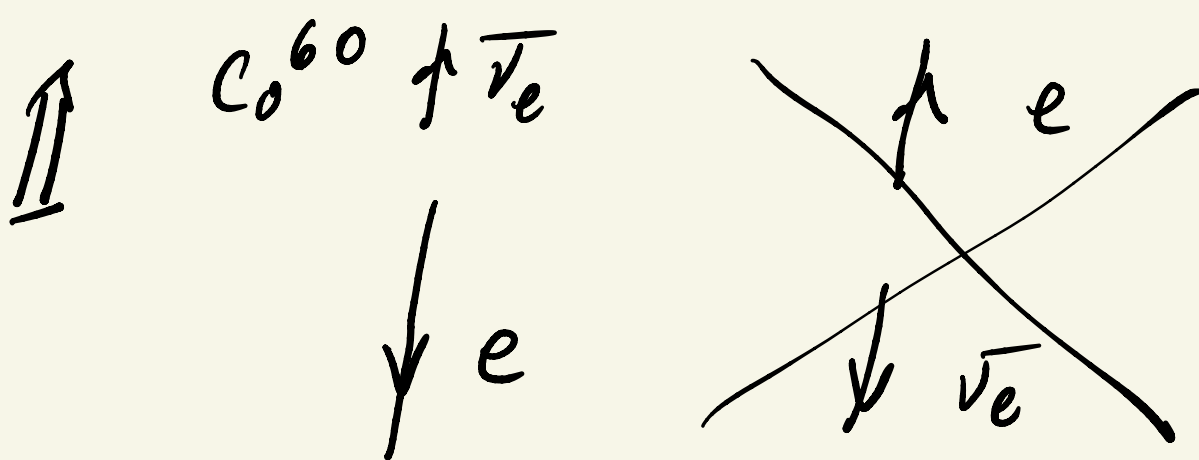
$$\# = 10^{13} 10^{-44} 10^{24} 10^5 / \text{sec}$$

$$\approx 10^{-2} / \text{sec} \approx 1 / \text{min}$$

Pauli: "All comes to who  
knows how to wait"

1956      Lee, Yang ( $\phi$ ?)  
June       $\longrightarrow$       December

exp: Maximal  $\phi$



1957 Marshak, Sudarshan '57

$$j_w^\mu = \bar{p} \gamma^\mu \frac{1 + \gamma_5}{2} u +$$

$$+ \bar{v} \gamma^\mu \frac{1 + \gamma_5}{2} e$$

$$= \bar{p}_L \gamma^\mu u_L + \bar{v}_L \gamma^\mu e_L$$

$$\boxed{\gamma_5^2 = 1}$$

$$L \equiv \frac{1 + \gamma_5}{2}, \quad R = \frac{1 - \gamma_5}{2}$$

$$L^2 = L, \quad R^2 = R, \quad LR = 0$$

$$\gamma = L\gamma + R\gamma = \gamma_L + \gamma_R$$

"V-A"

Wentzel 2009

"V-A was the key"



1961



1967

Glashow

Wentzel, Salam



$$SM = SU(2)_L \times U(1)_Y$$

of electro-weak int

(ew)



The rest is history

SM :  $u_\nu = 0$



BSM

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$$\{ \sigma_\mu, \sigma_\nu \} = 2g_{\mu\nu} \quad \mu = 0, 1, 2, 3$$

$$g_{\mu\nu} = \text{diag} (1, -1, -1, -1)$$

$$\{ \gamma_5, \gamma_\mu \} = 0 \quad + \quad \gamma_5^2 = 1$$